



UNIVERSITY
OF APPLIED SCIENCES

BASIC CONTROL SYSTEMS

05 SYSTEM ANALYSIS THROUGH TRANSFER FUNCTIONS

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WHERE STUDENTS MATTER



POLES AND ZEROS

Theorem The Fundamental Theorem of Algebra

Let $f(x) = \sum_{n=0}^k a_n x^n$ be a non-constant polynomial and $a_n \in \mathbb{C}$, then there exist a unique factorization such that:

$$f(x) = \sum_{n=0}^k a_n x^n = r_0 \prod_{i=1}^k (x - r_i)$$

This fundamental theorem of algebra enables us to obtain a unique decomposition of a irreducible rational polynomial transfer function.

Numerator
Denominator

Definition Poles

The value(s) of s such that the denominator $D(s) = 0$

Definition Zeros

The value(s) of s such that the numerator $N(s) = 0$

These guarantees: *the poles and zeros are either real or in complex conjugate pairs.*





TRANSFER FUNCTIONS

All coefficients a_n and b_m are real.

- Transfer functions can be written as:

$$\frac{Y(s)}{X(s)} = \frac{b_m s^m + b_{m-1} s^{m-1} + \dots + b_2 s^2 + b_1 s + b_0}{a_n s^n + a_{n-1} s^{n-1} + \dots + a_2 s^2 + a_1 s + a_0}$$

- Or as:

$$\frac{Y(s)}{X(s)} = \frac{b_m}{a_n} \cdot \frac{(s - z_1)(s - z_2) \dots (s - z_{m-1})(s - z_m)}{(s - p_1)(s - p_2) \dots (s - p_{n-1})(s - p_n)}$$

- Which is the same as:

$$H(s) = \frac{b_m \prod_{k=0}^m z_k}{a_n \prod_{q=0}^n p_q} \frac{(\frac{1}{z_1} s - 1)(\frac{1}{z_2} s - 1) \dots (\frac{1}{z_{m-1}} s - 1)(\frac{1}{z_m} s - 1)}{(\frac{1}{p_1} s - 1)(\frac{1}{p_2} s - 1) \dots (\frac{1}{p_{n-1}} s - 1)(\frac{1}{p_n} s - 1)}$$

$$= K_{DC} \cdot \frac{(\frac{1}{z_1} s - 1)(\frac{1}{z_2} s - 1) \dots (\frac{1}{z_{m-1}} s - 1)(\frac{1}{z_m} s - 1)}{(\frac{1}{p_1} s - 1)(\frac{1}{p_2} s - 1) \dots (\frac{1}{p_{n-1}} s - 1)(\frac{1}{p_n} s - 1)}$$

DC Gain





AN EXAMPLE

Input: x , Output: y ,

Assume 0 initial conditions.

Given an ODE:

$$\frac{d^2y}{dt^2} + 2\frac{dy}{dt} - 8y = 3\frac{dx}{dt} + 1x$$

We do the Laplace transform:

$$s^2Y + 2sY - 8Y = 3sX + 1X$$

Define transfer function H :

$$H(s) = \frac{Y(s)}{X(s)} = \frac{3s + 1}{s^2 + 2s - 8} = 3 \frac{s + \frac{1}{3}}{(s + 4)(s - 2)}$$



IDENTIFYING POLES AND ZEROS

$$H(s) = \frac{Y(s)}{X(s)} = \frac{1}{3} \frac{s + \frac{1}{3}}{(s + 4)(s - 2)}$$

According to the definitions:

Gain K	$\frac{1}{3}$
Zeros z	$-\frac{1}{3}$
Poles p	$-4, +2$

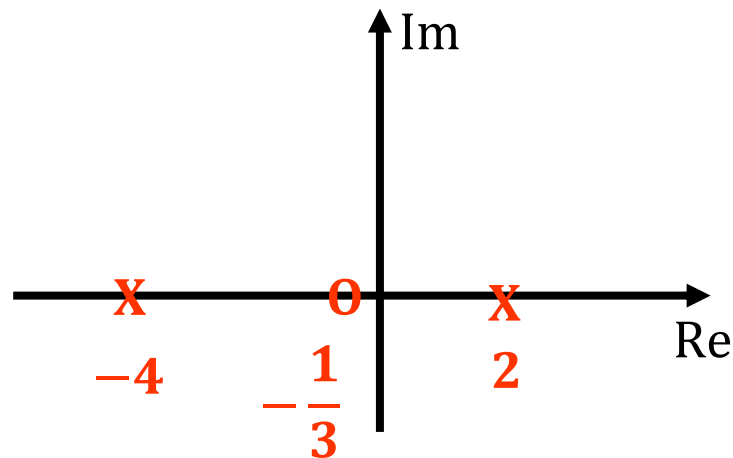
Obviously, when $s = -4$ or 2 (POLE), we have $H(s) \rightarrow \infty$

Obviously, when $s = -\frac{1}{3}$ (ZERO), we have $H(s) \rightarrow 0$

DRAWING POLES AND ZEROS IN THE COMPLEX PLANE

Components	Values	
Gain K	$\frac{1}{3}$	We don't draw this here.
Zeros $s = z$	$-\frac{1}{3}$	x
Poles $s = p$	$-4, +2$	o

s-domain





ADDITIONAL PROPERTY OF POLES AND ZEROS

We are modelling causal linear systems in the real world.



ADDITIONAL PROPERTY OF POLES AND ZEROS

We are modelling causal linear systems in the real world.

This simple sentence tells us a lot!



ADDITIONAL PROPERTY OF POLES AND ZEROS

We are modelling **causal linear systems** in the real world.

Number of zeros never
more than number of poles

The system can be
modeled by a *linear
inhomogeneous* ODE

All coefficients are real

The poles and zeros with non-zero imaginary components always
comes in **conjugate pairs**.

For all poles and zeros, if there exist a pole/zero $\sigma + j\omega$ with $\omega \neq 0$, there
must exist another pole/zero which is $\sigma - j\omega$ with $\omega \neq 0$ (the complex
conjugate).



CONTINUING OUR EXAMPLE

$$H(s) = \frac{Y(s)}{X(s)} = \frac{3s + 1}{s^2 + 2s - 8} = 3 \frac{s + \frac{1}{3}}{(s + 4)(s - 2)}$$

$$H(s) = \frac{\frac{11}{6}}{(s + 4)} + \frac{\frac{7}{6}}{(s - 2)}$$

Inverse Laplace transform:

$$h(t) = \frac{1}{6} (11e^{-4t} + 7e^{2t})$$

TRANSFORM -> DECOMPOSE

What did we just do?

The process function $h(t)$ can be decomposed to the summation of linearly independent exponentials: $Ce^{\lambda t}$

In fact, with Laplace transform, we can decompose any linear system into linearly independent exponentials:

$$h(t) = \sum C e^{\lambda t}$$



POLES ARE CRUCIAL

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The process function $h(t)$ can be decomposed to the summation of linearly independent exponentials: $Ce^{\lambda t}$

In fact, with Laplace transform, we can decompose any linear system into linearly independent exponentials:

$$h(t) = \sum C e^{\lambda t}$$

λ correspond to the **poles** of the transfer function.



POLES ARE CRUCIAL

λ correspond to the **poles** of the transfer function. So,

$$h(t) = \sum C e^{\lambda t} = \sum C e^{\sigma t} e^{j\omega t}$$

σ - determines the decay(if stable) of the output signal

ω – determines the oscillation of the output signal

POLES ARE CRUCIAL – RECALL EXAMPLE

$$H(s) = \frac{Y(s)}{X(s)} = \frac{3s + 1}{s^2 + 2s - 8} = 3 \frac{s + \frac{1}{3}}{(s + 4)(s - 2)}$$

$$H(s) = \frac{\frac{11}{6}}{(s + 4)} + \frac{\frac{7}{6}}{(s - 2)}$$

pole: -4 *pole: 2*

Inverse Laplace transform:

$$h(t) = \frac{1}{6} (11e^{-4t} + 7e^{2t})$$



STABILITY

Is $h(t)$ stable?

$$h(t) = \frac{1}{6} (11e^{-4t} + 7e^{2t})$$



STABILITY

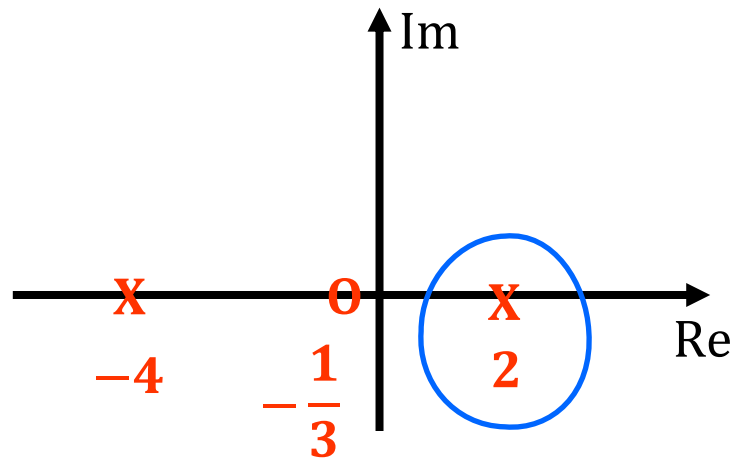
Is $h(t)$ stable?

$$h(t) = \frac{1}{6} (11e^{-4t} + 7e^{2t})$$

Obviously not, if we look at $h(t)$ as $t \rightarrow \infty$:

$$\lim_{t \rightarrow \infty} \frac{1}{6} (11e^{-4t} + 7e^{2t}) = 0 + \infty$$

So not stable!



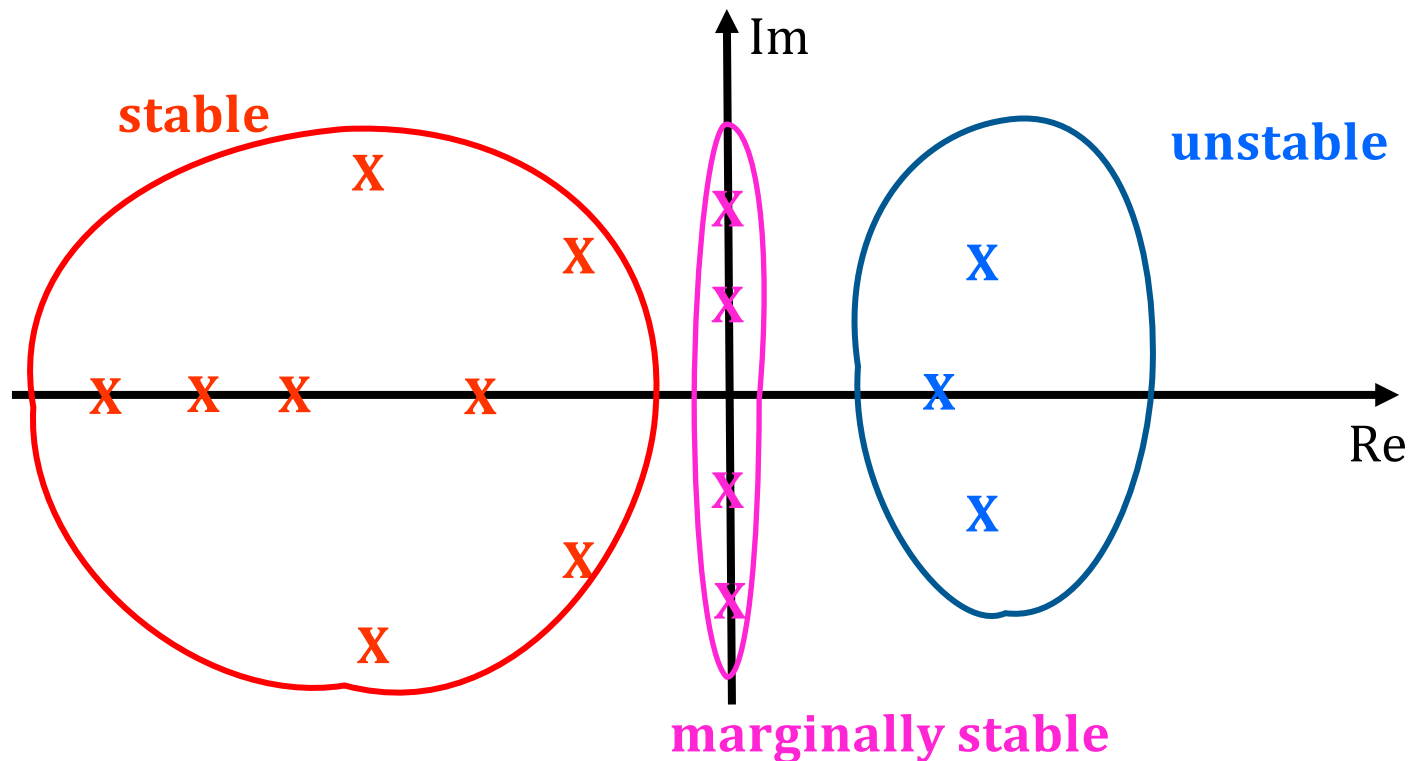


STABILITY CRITERIA

Left Half Plane

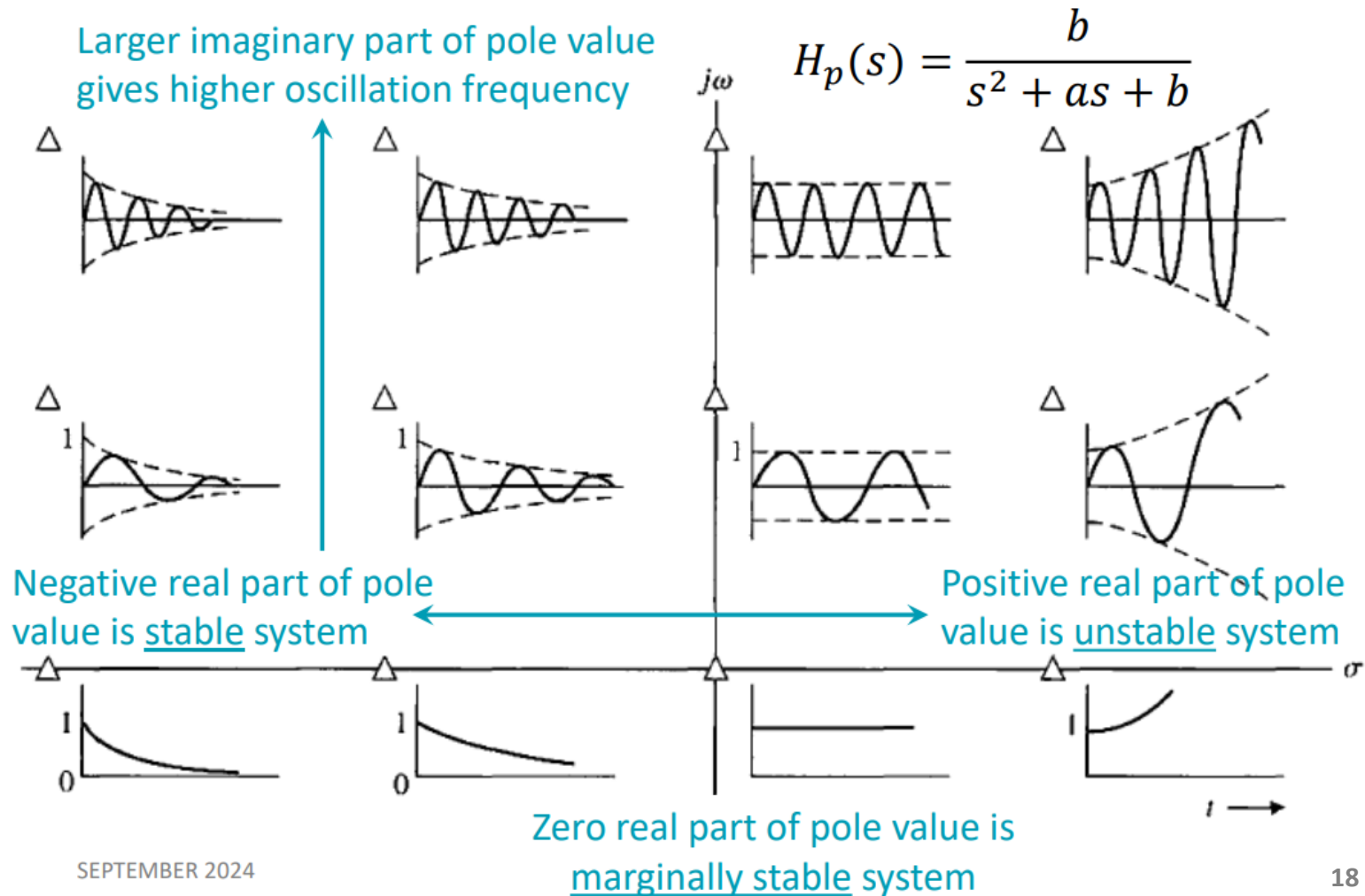
All poles should be in the open LHP of the s-plane.

iff $\forall \operatorname{Re}(p) < 0$, stable!



Larger imaginary part of pole value
gives higher oscillation frequency

$$H_p(s) = \frac{b}{s^2 + as + b}$$

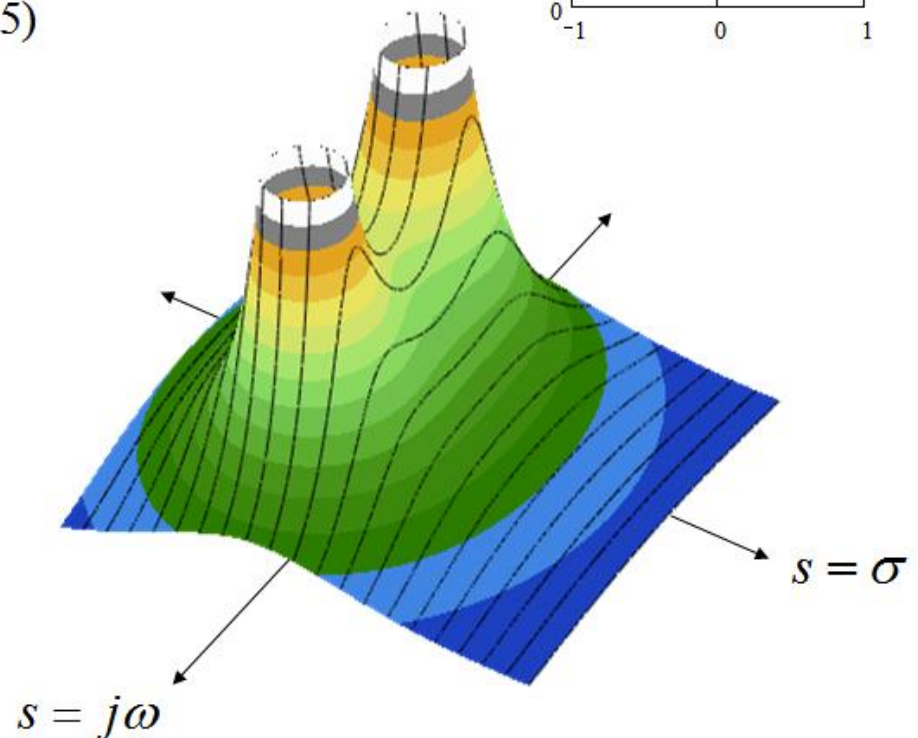
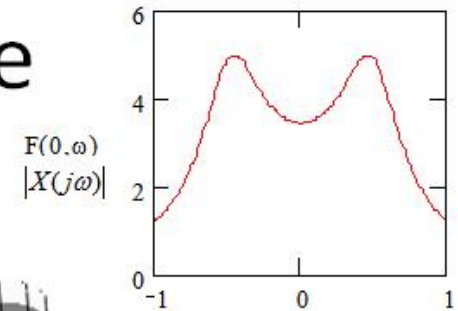
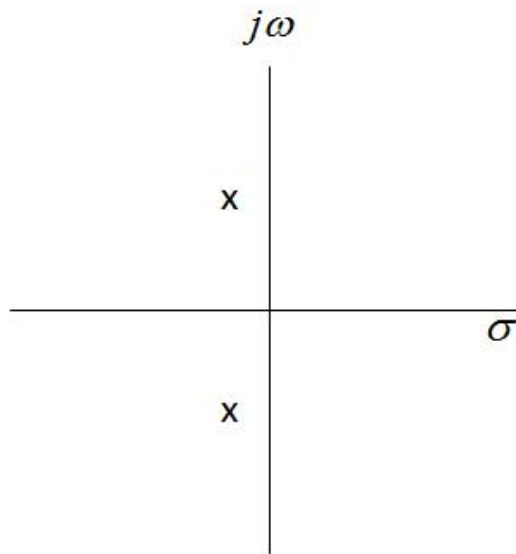


Poles and zeros: Why we care!

Filter Example

$$X(s) = \frac{1}{(s + .2 + j.5)(s + .2 - j.5)}$$

(poles at $s = -.2 \pm j.5$)

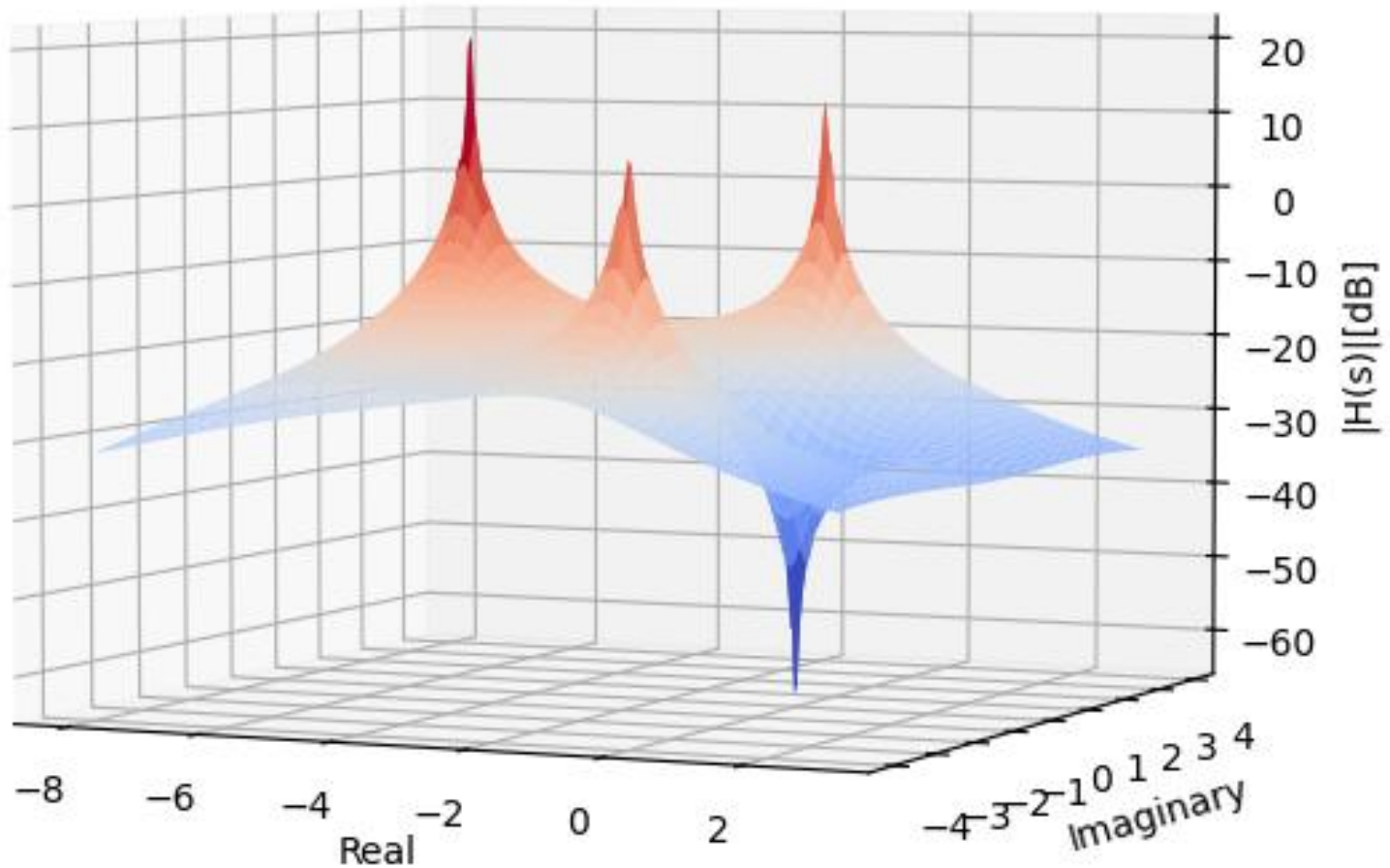




Poles and zeros: Why we care!

$$\frac{s}{(s+5)(s^2+2s+7)}$$

(Visualization in log scale)



SUMMARY

Transfer function:

$$H(s) = \frac{Y(s)}{X(s)}$$

Poles:

$s = p$ such that $X(s = p) = 0$, where $|H(s)| \rightarrow \infty$

Zeros:

$s = z$ such that $Y(s = z) = 0$, where $|H(s)| \rightarrow 0$

Stability criteria:

all poles in the open LHP



THE LAPLACE TRANSFORM OF A GENERAL PERIODIC FUNCTION

Define a general function $\gamma(t)$ defined in one time period T :

$$\gamma(t) = \begin{cases} f(t), & 0 < t < T \\ 0, & \text{otherwise} \end{cases}$$

We can write the periodic $f(t)$ as the delayed copies of $\gamma(t)$:

$$f(t) = \gamma(t - 0T) + \gamma(t - 1T) + \gamma(t - 2T) + \gamma(t - 3T) + \dots$$

Recall a single time shift in Laplace transform:

$$f(t - a) \Leftrightarrow e^{-as} \cdot F(s)$$

The Laplace transformed $F(s)$:

$$F(s) = \Gamma(s) \sum_{n=0}^{\infty} e^{-nTs}$$

Because we have $n, T > 0$ and $e^{-1} < 1$,
we may utilize the geometric series:

$$F(s) = \frac{1}{1 - e^{-sT}} \Gamma(s)$$



THE LAPLACE TRANSFORM OF A PERIODIC FUNCTION

$$F(s) = \frac{1}{1 - e^{-sT}} \Gamma(s)$$

When we have a sampling frequency $\omega_0 = \frac{1}{T}$, $F(s)$ becomes:

$$F(s) = \frac{1}{1 - e^{-\frac{s}{\omega_0}}} \Gamma(s)$$

This periodic time shifting creates “a pole” in addition to the $\Gamma(s)$?!

As $\frac{\omega}{\omega_0} \rightarrow 0 + 2k\pi$, $k \in \mathbb{Z}$, we may obtain the pole:

$$\frac{1}{1 - e^{-j\frac{\omega}{\omega_0}}} \rightarrow \frac{1}{0} \rightarrow \infty$$



HOMework

Stage ONE exercises:

- Problem 1
- Problem 4



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SELF-READING

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WHERE STUDENTS MATTER

Determination of the poles and zeros

- Step 1: rewrite the transfer function in such a way that the coefficient of the highest power becomes 1 (both for zeros and poles!)

– Examples:

Coefficient in the numerator is 0.1

$$G(s) = \frac{0,1s + 1}{s^2 + 7s + 12} =$$

Denominator coefficient of the highest power already is 1

Determination of the poles and zeros

- Step 1: rewrite the transfer function in such a way that the coefficient of the highest power becomes 1 (both for zeros and poles!)
 - Examples:

$$G(s) = \frac{0,1s + 1}{s^2 + 7s + 12} = \frac{0,1(s + 10)}{s^2 + 7s + 12} =$$

Determination of the poles and zeros

- Step 1: rewrite the transfer function in such a way that the coefficient of the highest power becomes 1 (both for zeros and poles!)
 - Examples:

$$G(s) = \frac{0,1s + 1}{s^2 + 7s + 12} = \frac{0,1(s + 10)}{s^2 + 7s + 12} = \frac{1}{10} \cdot \frac{s + 10}{s^2 + 7s + 12}$$



Determination of the poles and zeros

- Step 1: rewrite the transfer function in such a way that the coefficient of the highest power becomes 1 (both for zeros and poles!)
 - Examples:

$$G(s) = \frac{0,1s + 1}{s^2 + 7s + 12} = \frac{0,1(s + 10)}{s^2 + 7s + 12} = \frac{1}{10} \cdot \frac{s + 10}{s^2 + 7s + 12}$$

$$G(s) = \frac{3s + 30}{5s^2 + 15s + 250} =$$

Determination of the poles and zeros

- Step 1: rewrite the transfer function in such a way that the coefficient of the highest power becomes 1 (both for zeros and poles!)
 - Examples:

$$G(s) = \frac{0,1s + 1}{s^2 + 7s + 12} = \frac{0,1(s + 10)}{s^2 + 7s + 12} = \frac{1}{10} \cdot \frac{s + 10}{s^2 + 7s + 12}$$

$$G(s) = \frac{3s + 30}{5s^2 + 15s + 250} = \frac{3(s + 10)}{5(s^2 + 3s + 50)} = \frac{3}{5} \cdot \frac{s + 10}{s^2 + 3s + 50}$$

Poles and zeros construction steps

- Step 1: rewrite the transfer function in such a way that the coefficient of the highest power becomes 1
- Step 2: rewrite the transfer function in its base parts – a constant, poles and zeros

$$G(s) = \frac{1}{10} \cdot \frac{s+10}{s^2 + 7s + 12} = \frac{1}{10} \cdot \frac{s+10}{(s+3)(s+4)}$$

Poles and zeros construction steps

- Step 1: rewrite the transfer function in such a way that the coefficient of the highest power becomes 1
- Step 2: rewrite the transfer function in its base parts – a constant, poles and zeros

$$G(s) = \frac{1}{10} \cdot \frac{s+10}{s^2 + 7s + 12} = \frac{1}{10} \cdot \frac{s+10}{(s+3)(s+4)}$$

$$G(s) = \frac{3}{5} \cdot \frac{s+10}{s^2 + 3s + 50} =$$

Sometimes the solution is complex
→ results in two complex poles



Poles and zeros construction steps

- Step 1: rewrite the transfer function in such a way that the coefficient of the highest power becomes 1
- Step 2: rewrite the transfer function in its base parts – a constant, poles and zeros

$$G(s) = \frac{1}{10} \cdot \frac{s+10}{s^2 + 7s + 12} = \frac{1}{10} \cdot \frac{s+10}{(s+3)(s+4)}$$

$$G(s) = \frac{3}{5} \cdot \frac{s+10}{s^2 + 3s + 50} = \frac{3}{5} \cdot \frac{s+10}{(s + \frac{3}{2} + \frac{13,8}{2} j)(s + \frac{3}{2} - \frac{13,8}{2} j)}$$

Sometimes the solution is complex
→ results in two complex poles

Poles and zeros construction steps

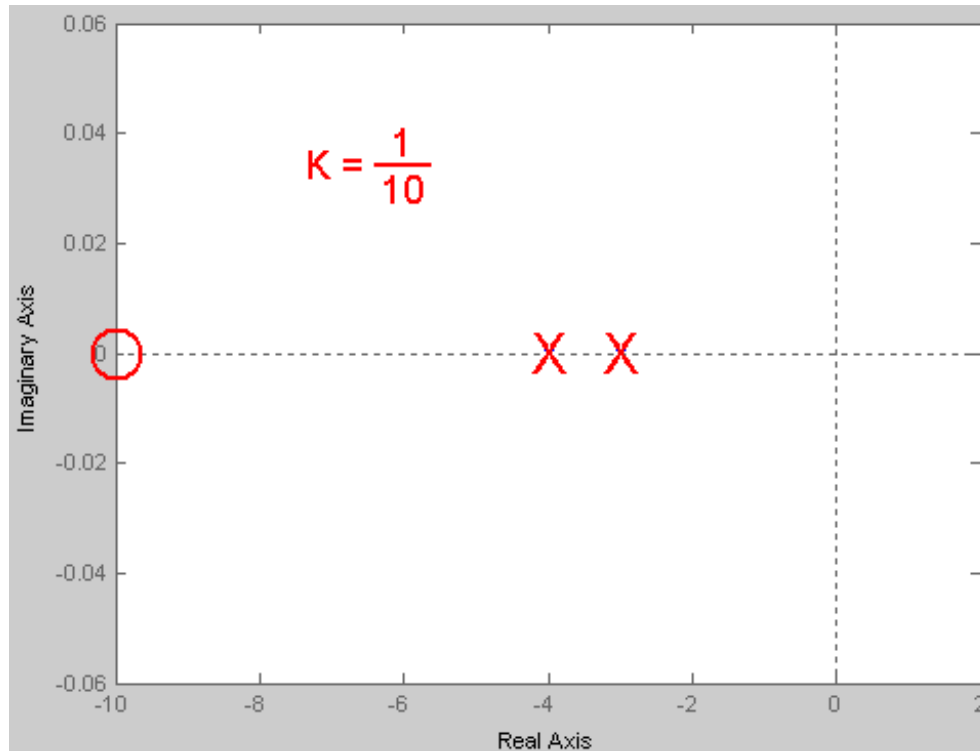
- Step 1: rewrite the transfer function in such a way that the coefficient of the highest power becomes 1
- Step 2: rewrite the transfer function in its base parts – a constant, poles and zeros
- Step 3: draw the poles and zeros in the (complex) s-plane; the constant is mentioned separately as K



Poles and zeros example

- Step 3: draw the poles and zeros in the (complex) s-plane; the constant is mentioned separately as K

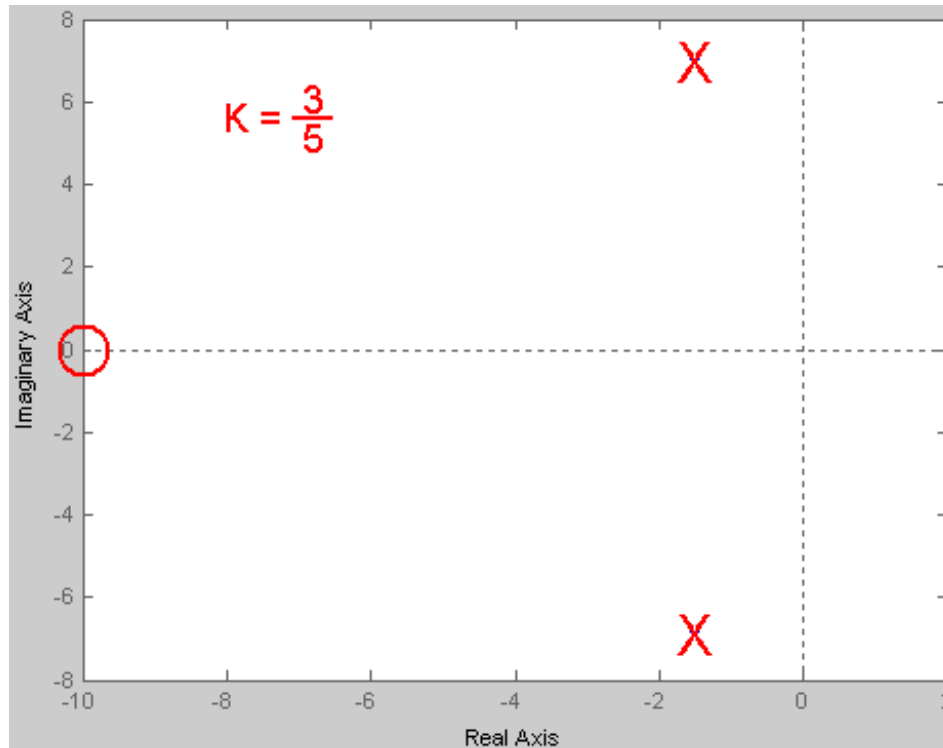
$$G(s) = \frac{1}{10} \cdot \frac{s+10}{(s+3)(s+4)}$$





Poles and zeros example

$$G(s) = \frac{3}{5} \cdot \frac{s+10}{(s + \frac{3}{2} + \frac{13,8}{2} j)(s + \frac{3}{2} - \frac{13,8}{2} j)}$$





Poles and zeros exercises

Draw the poles and zeros in the s-plane for:

1.
$$H(s) = \frac{25s + 3}{4s^2 + 9s + 2}$$

2.
$$H(s) = \frac{3s + 4}{s^2 + 6s + 8}$$

3.
$$H(s) = \frac{2s + 1}{s^2 + 4s + 8}$$



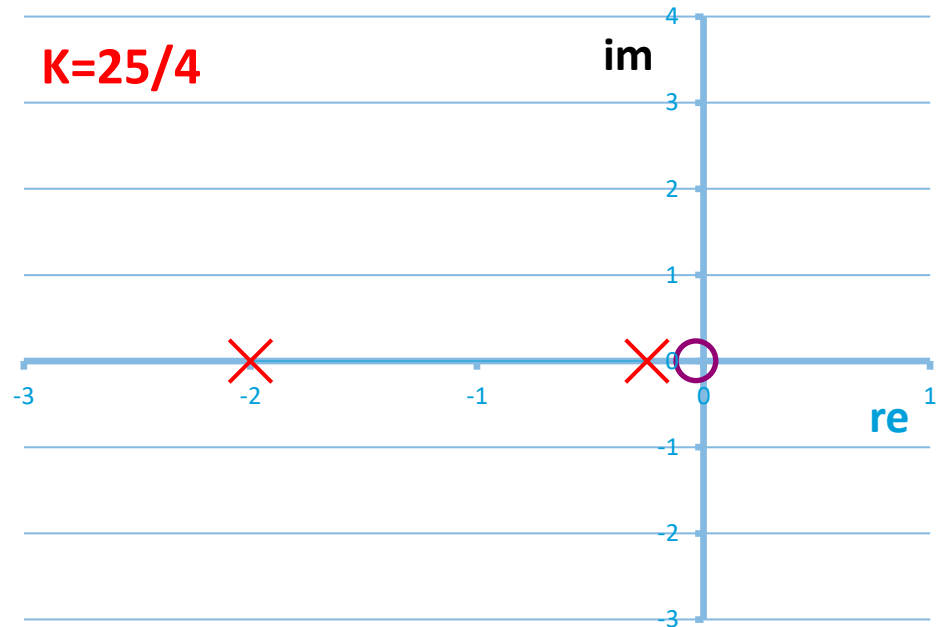


Poles and zeros exercises

- Draw the poles and zeros in the s-plane for:

1. $H(s) = \frac{25s + 3}{4s^2 + 9s + 2}$

- zero: $-3/25$
- poles: $-1/4$ and -2
- $K = 25/4$



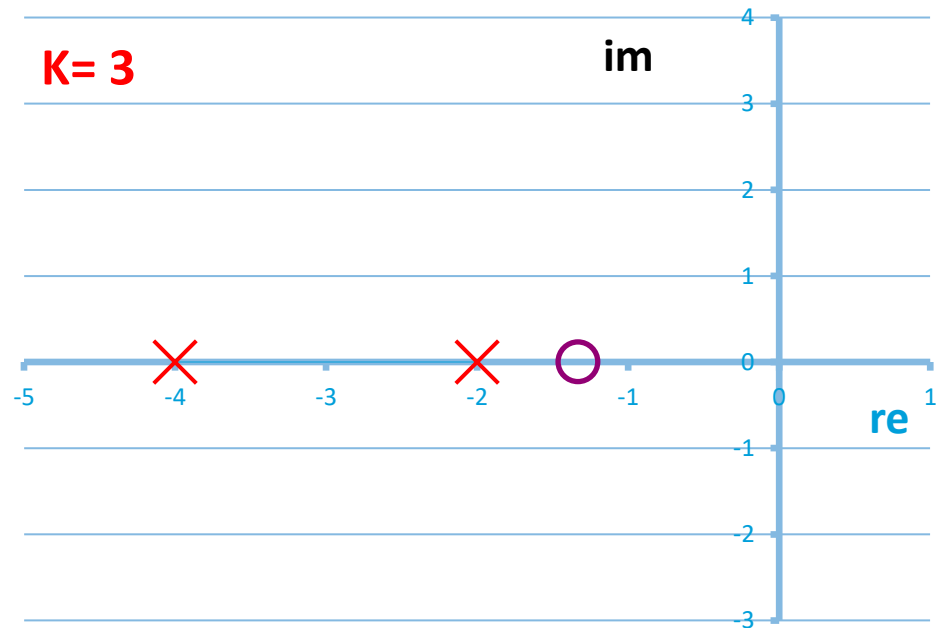


Poles and zeros exercises

- Draw the poles and zeros in the s-plane for:

2. $H(s) = \frac{3s + 4}{s^2 + 6s + 8}$

- zeros: $-4/3$
- poles: -2 and -4
- $K = 3$



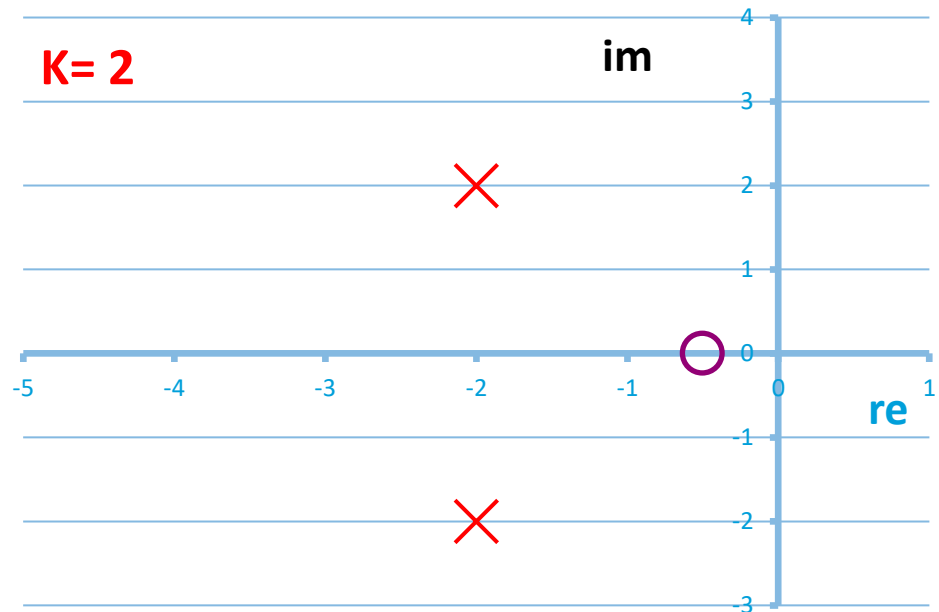


Poles and zeros exercises

- Draw the poles and zeros in the s-plane for:

3. $H(s) = \frac{2s + 1}{s^2 + 4s + 8}$

- zeros: $-1/2$
- poles: $-2+2j$
and $-2-2j$
- $K = 2$





Poles and zeros exercises

4. Draw in the s-plane the poles and zeros of the transfer function $H(s) = X(s)/F(s)$ and:

$$\frac{d^4 x(t)}{dt^4} + 2 \frac{d^3 x(t)}{dt^3} + 2 \frac{d^2 x(t)}{dt^2} = \frac{df(t)}{dt} + f(t)$$

All values at time = 0 are zero
(so $x'''(0)=x''(0)=0$, etc.).



Poles and zeros exercises

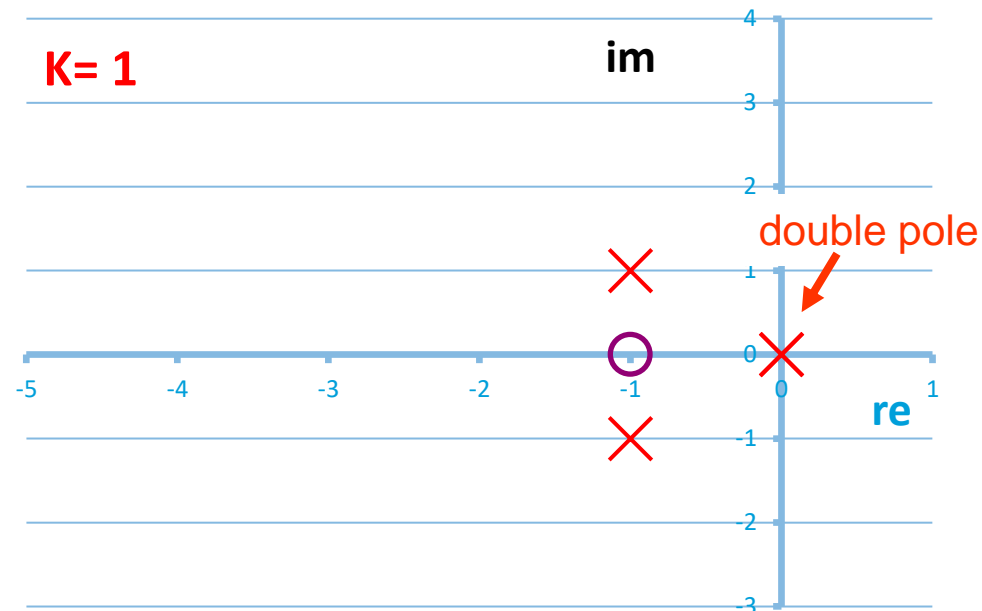
- Draw the poles and zeros in the s-plane for:

4.
$$\frac{d^4 x(t)}{dt^4} + 2 \frac{d^3 x(t)}{dt^3} + 2 \frac{d^2 x(t)}{dt^2} = \frac{df(t)}{dt} + f(t)$$

Laplace $\rightarrow s^4 + 2s^3 + 2s^2 = s + 1$

Transfer function:

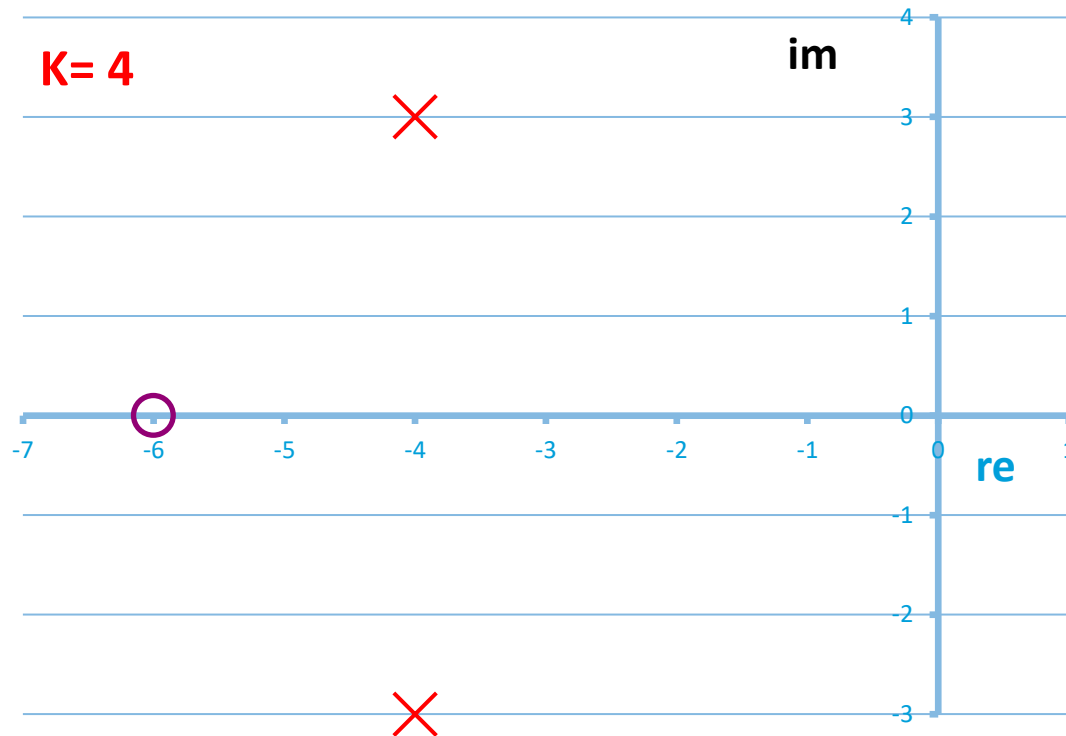
$$H_s = \frac{s + 1}{s^4 + 2s^3 + 2s^2}$$
$$= \frac{s + 1}{s * s(s + 1 + j)(s + 1 - j)}$$





Poles and zeros exercises

5. Find the differential equation for:



Assume that the initial conditions are zero.
Input is $x(t)$ and output is $y(t)$.



Poles and zeros exercises

5. Find the differential equation



$$\frac{Y(s)}{X(s)} = 4 \frac{s + 6}{(s + 4 - 3i)(s + 4 + 3i)}$$

Poles and zeros exercises

5. Find the differential equation



$$\frac{Y(s)}{X(s)} = 4 \frac{s + 6}{(s + 4 - 3i)(s + 4 + 3i)} = \frac{4s + 24}{s^2 + 8s + 25}$$



Poles and zeros exercises

5. Find the differential equation



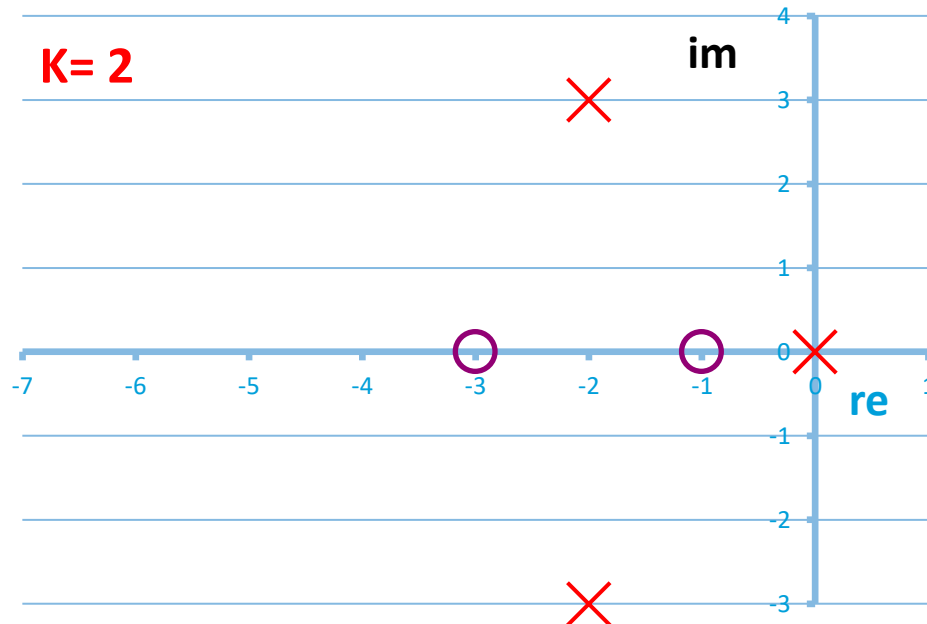
$$\frac{Y(s)}{X(s)} = 4 \frac{s + 6}{(s + 4 - 3i)(s + 4 + 3i)} = \frac{4s + 24}{s^2 + 8s + 25}$$

$$\frac{d^2 y(t)}{dt^2} + 8 \frac{dy(t)}{dt} + 25y = 4 \frac{dx(t)}{dt} + 24x(t)$$



Poles and zeros exercises

6. Find the differential equation for:



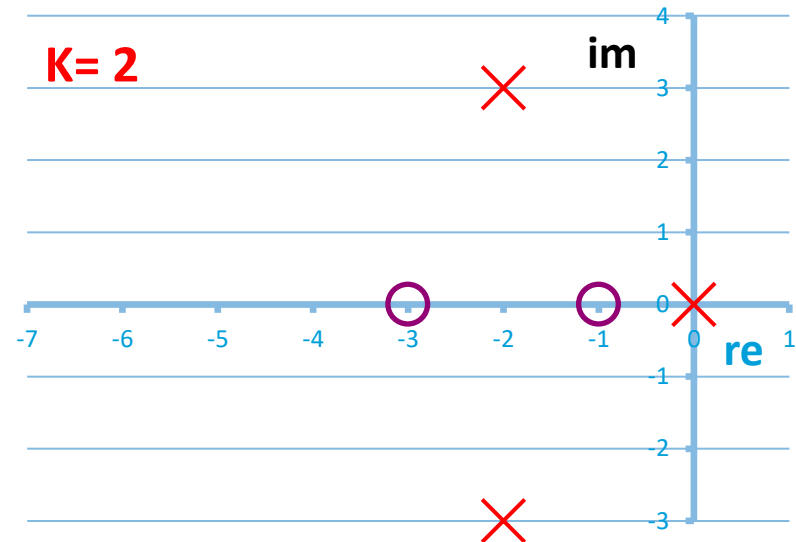
Assume that the initial conditions are zero.
Input is $x(t)$ and output is $y(t)$.



Poles and zeros exercise

6. Find the differential equation

$$\frac{Y(s)}{X(s)} = 2 \frac{(s+1)(s+3)}{(s+2-3i)(s+2+3i)s}$$



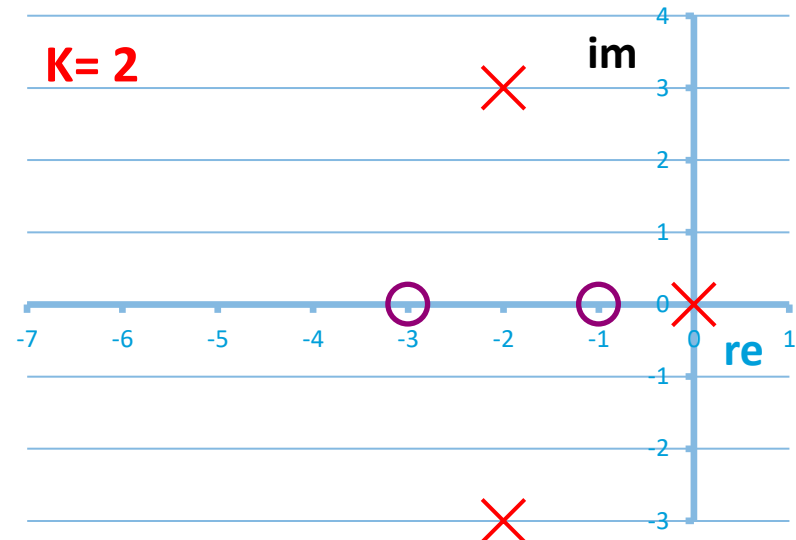


Poles and zeros exercise

6. Find the differential equation

$$\frac{Y(s)}{X(s)} = 2 \frac{(s+1)(s+3)}{(s+2-3i)(s+2+3i)s}$$

$$\frac{Y(s)}{X(s)} = \frac{2s^2 + 8s + 6}{s^3 + 4s^2 + 13s}$$



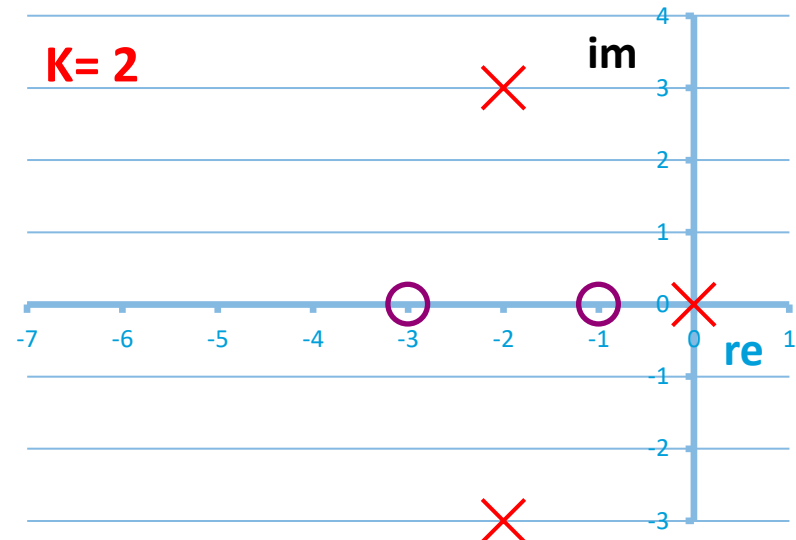


Poles and zeros exercise

6. Find the differential equation

$$\frac{Y(s)}{X(s)} = 2 \frac{(s+1)(s+3)}{(s+2-3i)(s+2+3i)s}$$

$$\frac{Y(s)}{X(s)} = \frac{2s^2 + 8s + 6}{s^3 + 4s^2 + 13s}$$



$$\frac{d^3 y(t)}{dt^3} + 4 \frac{d^2 y(t)}{dt^2} + 13 \frac{dy(t)}{dt} = 2 \frac{d^2 x(t)}{dt^2} + 8 \frac{dx(t)}{dt} + 6x(t)$$

Poles and zeros exercise

7. Draw the poles and zeros in the s-plane for the combination:

$$\frac{d^2 y(t)}{dt^2} + 8 \frac{dy(t)}{dt} + 15y(t) = 5 \frac{dx(t)}{dt} + 10x(t)$$

$$x(t) = 2t$$



Poles and zeros exercises

7. Draw the poles and zeros in the s-plane for the combination:

$$\frac{d^2 y(t)}{dt^2} + 8 \frac{dy(t)}{dt} + 15y(t) = 5 \frac{dx(t)}{dt} + 10x(t) \quad \rightarrow$$

$$x(t) = 2t \quad \rightarrow$$

**Laplace
Transform**



Poles and zeros exercises

7. Draw the poles and zeros in the s-plane for the combination:

$$\frac{d^2 y(t)}{dt^2} + 8 \frac{dy(t)}{dt} + 15y(t) = 5 \frac{dx(t)}{dt} + 10x(t) \quad \Rightarrow \quad H(s) = \frac{5s + 10}{s^2 + 8s + 15}$$

$$x(t) = 2t \quad \Rightarrow \quad X(s) = \frac{2}{s^2}$$

$$H(s) = Y(s)/X(s) \rightarrow Y(s) = H(s) \cdot X(s)$$



Poles and zeros exercises

7. Draw the poles and zeros in the s-plane for the combination:

$$\frac{d^2 y(t)}{dt^2} + 8 \frac{dy(t)}{dt} + 15y(t) = 5 \frac{dx(t)}{dt} + 10x(t) \Rightarrow H(s) = \frac{5s + 10}{s^2 + 8s + 15}$$

$$x(t) = 2t \Rightarrow X(s) = \frac{2}{s^2}$$

$$Y(s) = \frac{10s + 20}{s^2(s^2 + 8s + 15)}$$

$$Y(s) = 10 \frac{s + 2}{s^2(s + 3)(s + 5)}$$



Poles and zeros exercises

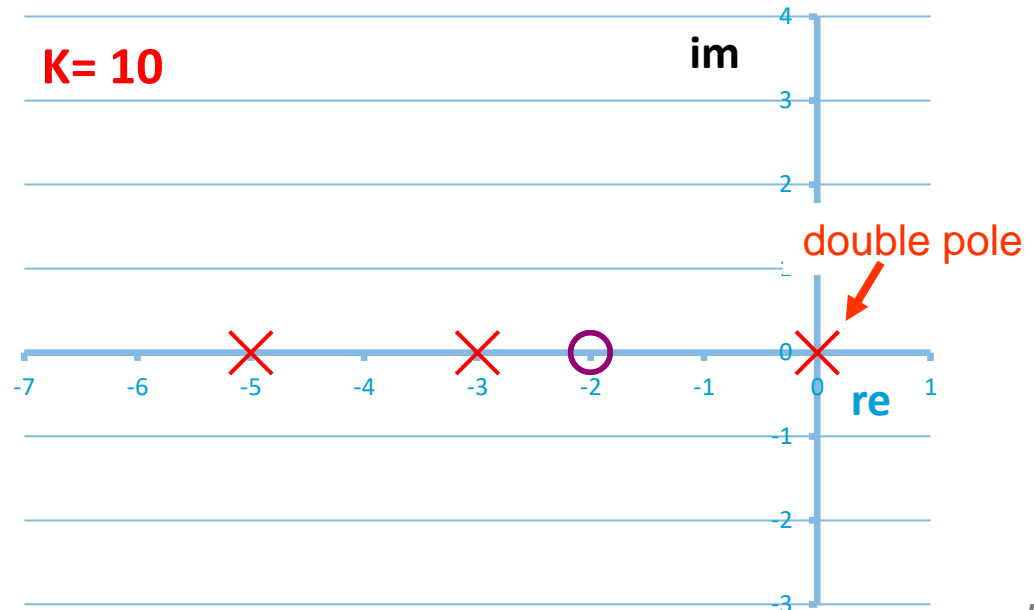
7. Draw the poles and zeros in the s-plane for the combination:

$$\frac{d^2 y(t)}{dt^2} + 8 \frac{dy(t)}{dt} + 15y(t) = 5 \frac{dx(t)}{dt} + 10x(t) \Rightarrow H(s) = \frac{5s + 10}{s^2 + 8s + 15}$$

$$x(t) = 2t \Rightarrow X(s) = \frac{2}{s^2}$$

$$Y(s) = \frac{10s + 20}{s^2(s^2 + 8s + 15)}$$

$$Y(s) = 10 \frac{s + 2}{s^2(s + 3)(s + 5)}$$



Poles and zeros exercises

8. Draw the poles and zeros in the s-plane for the combination:

$$\frac{d^2 y(t)}{dt^2} + 5 \frac{dy(t)}{dt} + 4y(t) = 3 \frac{dx(t)}{dt} + 18x(t)$$

$$x(t) = 5 \cos(3t)$$



Poles and zeros exercises

8. Draw the poles and zeros in the s-plane for the combination:

$$\frac{d^2 y(t)}{dt^2} + 5 \frac{dy(t)}{dt} + 4y(t) = 3 \frac{dx(t)}{dt} + 18x(t) \quad \rightarrow$$

$$x(t) = 5 \cos(3t) \quad \rightarrow$$

Laplace
Transform



Poles and zeros exercises

8. Draw the poles and zeros in the s-plane for the combination:

$$\frac{d^2 y(t)}{dt^2} + 5 \frac{dy(t)}{dt} + 4y(t) = 3 \frac{dx(t)}{dt} + 18x(t) \quad \Rightarrow \quad H(s) = \frac{3s + 18}{s^2 + 5s + 4}$$

$$x(t) = 5 \cos(3t) \quad \Rightarrow \quad X(s) = 5 \frac{s}{s^2 + 9}$$

Laplace
Transform



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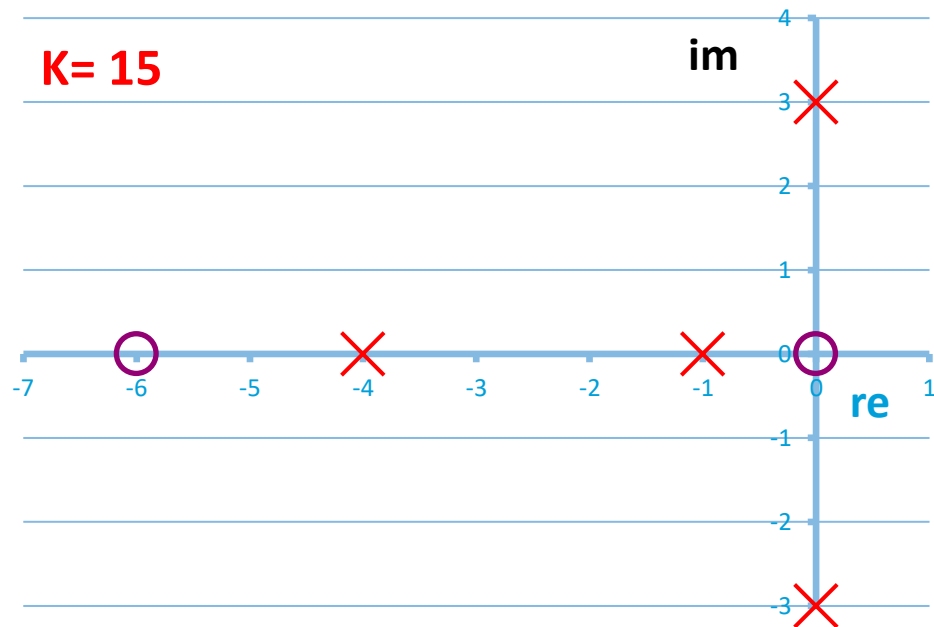
$$Y(s) = 15 \frac{s(s + 6)}{(s + 1)(s + 4)(s + 3j)(s - 3j)}$$



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Matlab commands

$$H_s = \frac{(s + 7)}{s(s + 5)(s + 15)}$$

Define a system:

You can use:

```
>> sys=zpk(-7,[0 -5 -15],1);
```

or

```
>> sys=tf([1 7],[1 20 75 0]);
```

Another option is

```
>> s=tf('s');
```

```
>> sys= (s+7)/(s*(s+5)*(s+15));
```

Look at location of poles and zeros

```
>> pzmap(sys)
```

```
>> ltiview(sys)
```

